## Amendments to the Claims:

This listing of claims will replace all prior versions, and listings, of claims in the application:

## Listing of Claims:

(Currently Amended) A linear method for performing head 1 1. motion estimation from facial feature data, the method comprising 2 the steps of: obtaining a first facial image and detecting a head in said first image; detecting position of not more than only four points P of said 6 first facial image where  $P = \{\mathbf{p}_1, \mathbf{p}_2, \mathbf{p}_3, \mathbf{p}_4\}$ , and  $\mathbf{p}_k = \{x_k, y_k\}$ ; 7 8 obtaining a second facial image and detecting a head in said second image; 10 detecting position of not more than only four points P' of said first second facial image where  $P' = \{p'_1, p'_2, p'_3, p'_4\}$  and  $p'_k = (x'_k, y'_k)$ ; 11 and 12

13

14

determining the motion of the head represented by a rotation

matrix R and translation vector T using said points P and P'.

- 1 2. (Currently Amended) The linear method of claim 1, wherein
- 2 said cnly four points P of said first facial image and said only
- 3 four points P' of said second facial image include locations of
- 4 outer corners of each eye and mouth of each respective first and
- 5 second facial images.
- 1 3. (Original) The linear method of claim 1, wherein said
- 2 head motion estimation is governed according to:
- 3  $\mathbf{P}_i' = R\mathbf{P}_i + \mathbf{T}, \text{ where } R = \begin{bmatrix} \mathbf{r}_1^T \\ \mathbf{r}_2^T \\ \mathbf{r}_3^T \end{bmatrix} = \begin{bmatrix} r_{ij} \end{bmatrix}_{3\times3} \text{ and } \mathbf{T} = \begin{bmatrix} T_1 & T_2 & T_3 \end{bmatrix}^T \text{ represent camera}$
- 4 rctation and translation respectively, said head pose estimation
- 5 being a specific instance of head motion estimation.
- 1 4. (Currently amended) A linear method for performing head
- 2 motion estimation from facial feature data, the method comprising
- 3 the steps of:
- obtaining a first facial image and detecting a head in said
- 5 first image;
- detecting position of four points P of said first facial image
- 7 where  $P = \{p_1, p_2, p_3, p_4\}$ , and  $p_k = (x_k, y_k)$ ;
- obtaining a second facial image and detecting a head in said
- 9 second image;

- detecting position of four points P' of said first second
- 11 facial image where  $P' = \{p'_1, p'_2, p'_3, p'_4\}$  and  $p'_k = (x'_k, y'_k)\}$ ; and,
- determining the motion of the head represented by a rotation
- matrix R and translation vector T using said points P and P',
- wherein said head motion estimation is governed according to:

15 
$$\mathbf{P}_{i}' = R\mathbf{P}_{i} + \mathbf{T}, \text{ where } R = \begin{bmatrix} \mathbf{r}_{1}^{T} \\ \mathbf{r}_{2}^{T} \\ \mathbf{r}_{3}^{T} \end{bmatrix} = \begin{bmatrix} r_{ij} \end{bmatrix}_{3\times3} \text{ and } \mathbf{T} = \begin{bmatrix} T_{1} & T_{2} & T_{3} \end{bmatrix}^{T} \text{ represent camera}$$

- 16 rotation and translation respectively, said head pose estimation
- 17 being a specific instance of head motion estimation, and
- wherein said head motion estimation is governed according to
- 19 said rotation matrix R, said method further comprising the steps
- 20 of:
- determining rotation matrix R that maps points  $P_k$  to  $F_k$  for
- characterizing a head pose, said points  $\mathbf{F_1},\mathbf{F_2},\mathbf{F_3},\mathbf{F_4}$  representing three-
- 23 dimensional (3-D) coordinates of the respective four points of a
- 24 reference, frontal view of said facial image, and  $\mathbf{P_k}$  is the three-
- 25 dimensional (3-D) coordinates of an arbitrary point where
- P<sub>i</sub> =  $[X_i \ Y_i \ Z_i]^T$ , said mapping governed according to the relation:

$$R(\mathbf{P}_2 - \mathbf{P}_1) \propto \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}^T$$

$$R(\mathbf{P}_6 - \mathbf{P}_5) \propto \begin{bmatrix} 0 & 1 & 0 \end{bmatrix}^T$$

3

- wherein  $P_5$  and  $P_6$  are midpoints of respective line segments
- 31 connecting points  $P_1P_2$  and  $P_3P_4$  and, line segment connecting points
- 32  $P_1P_2$  is orthogonal to a line segment connecting points  $P_5P_6$ , and
- 33 <sup>∞</sup>indicates a proportionality factor.
- 5. (Original) The linear method of claim 4, wherein
- 2 components r1, r2 and r3 are computed as:

$$\mathbf{r}_2^T(\mathbf{P}_2 - \mathbf{P}_1) = 0$$

$$\mathbf{r}_{3}^{T}(\mathbf{P}_{2}-\mathbf{P}_{1})=0$$

$$\mathbf{r}_1^T(\mathbf{P}_6 - \mathbf{P}_5) = 0$$

$$\mathbf{r}_3^T(\mathbf{P}_6 - \mathbf{P}_5) = 0$$

- 1 6. (Original) The linear method of claim 5, wherein
- 2 components r1, r2 and r3 are computed as:

3 
$$\mathbf{r}_3 = (\mathbf{P}_6 - \mathbf{P}_5) \times (\mathbf{P}_2 - \mathbf{P}_1)$$
,

$$\mathbf{r}_2 = \mathbf{r}_3 \times (\mathbf{P}_2 - \mathbf{P}_1)$$

$$\mathbf{r}_1 = \mathbf{r}_2 \times \mathbf{r}_3$$

7. (Original) The linear method of claim 4, wherein

$$\begin{bmatrix} \mathbf{P}_{i}^{T} & \mathbf{0}^{T} & \mathbf{0}^{T} & 1 & 0 & 0 \\ \mathbf{0}^{T} & \mathbf{P}_{i}^{T} & \mathbf{0}^{T} & 0 & 1 & 0 \\ \mathbf{0}^{T} & \mathbf{0}^{T} & \mathbf{P}_{i}^{T} & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \mathbf{r}_{1} \\ \mathbf{r}_{2} \\ \mathbf{r}_{3} \\ \mathbf{T} \end{bmatrix} = \mathbf{P}_{i}^{T}$$

2

US010476-aaf-09-16-05.doc

- each point pair yielding 3 equations, whereby at least four
- 4 point pairs are necessary to linearly solve for said rotation and
- 5 translation.
- 1 8. (Original) The linear method of claim 7, further
- 2 comprising the step of: decomposing said rotation matrix R using
- 3 Singular Value Decomposition (SVD) to obtain a form  $R = USV^{T}$ .
- 9. (Original) The linear method of claim 7, further
- 2 comprising the step of computing a new rotation matrix according to
- $R = UV^T$
- 1 10. (Original) A linear method for performing head motion
- 2 estimation from facial feature data, the method comprising the
- 3 steps of:
- obtaining image position of four points  $\mathbf{p}_k$  of a facial image;
- determining a rotation matrix R that maps points  $\mathbf{P}_k$  to  $\mathbf{F}_k$  for
- characterizing a head pose, said points  $\mathbf{F}_1, \mathbf{F}_2, \mathbf{F}_3, \mathbf{F}_4$  representing
- 7 three-dimensional (3-D) coordinates of the respective four points
- 8 of a reference, frontal view of said facial image, and  $\mathbf{P}_k$  is the

- 9 three-dimensional (3-D) coordinates of an arbitrary point where
- $\mathbf{P}_i = [X_i \ Y_i \ Z_i]^T$ , said mapping governed according to the relation:

$$R(\mathbf{P}_2 - \mathbf{P}_1) \propto \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}^T$$

$$R(\mathbf{P}_6 - \mathbf{P}_5) \propto \begin{bmatrix} 0 & 1 & 0 \end{bmatrix}^T$$

13

- wherein  $P_5$  and  $P_6$  are midpoints of respective line segments
- connecting points  $P_1P_2$  and  $P_3P_4$  and, line segment connecting points
- 16  $P_1P_2$  is orthogonal to a line segment connecting points  $P_5P_6$ , and
- $\alpha$  indicates a proportionality factor.
- 1 11. (Original) The linear method of claim 10, wherein
- 2 components r1, r2 and r3 are computed as:

$$\mathbf{r}_2^T(\mathbf{P}_2 - \mathbf{P}_1) = 0$$

$$\mathbf{r}_3^T(\mathbf{P}_2 - \mathbf{P}_1) = 0$$

$$\mathbf{r_1}^r(\mathbf{P_6} - \mathbf{P_5}) = 0$$

$$\mathbf{r}_3^T(\mathbf{P}_6 - \mathbf{P}_5) = 0$$

- 1 12. (Original) The linear method of claim 12, wherein
- 2 components r1, r2 and r3 are computed as:

$$r_3 = (P_6 - P_5) \times (P_2 - P_1)$$

$$\mathbf{r}_2 = \mathbf{r}_3 \times (\mathbf{P}_2 - \mathbf{P}_1)$$

$$\mathbf{r}_1 = \mathbf{r}_2 \times \mathbf{r}_3$$

US010476-aaf-09-16-05.doc

- 1 13. (Original) The linear method of claim 12, wherein a
- 2 motion of head points is represented according to  $P'_i = RP_i + T$

$$R = \begin{bmatrix} \mathbf{r}_1^T \\ \mathbf{r}_2^T \\ \mathbf{r}_2^T \end{bmatrix} = [r_{ij}]_{3\times 3}$$

- $_3$  where  $\begin{bmatrix} \mathbf{r}_3 \end{bmatrix}$
- represents image rotation,  $T = \begin{bmatrix} T_1 & T_2 & T_3 \end{bmatrix}^T$
- 4 represents translation, and  $\mathbf{P}_l'$  denotes a 3-D image position of four
- 5 points  $P_k$  of another facial image
- 1 14. (Original) The linear method of claim 13, wherein

$$2 \qquad \begin{bmatrix} \mathbf{P}_{i}^{T} & \mathbf{0}^{T} & \mathbf{0}^{T} & 1 & 0 & 0 \\ \mathbf{0}^{T} & \mathbf{P}_{i}^{T} & \mathbf{0}^{T} & 0 & 1 & 0 \\ \mathbf{0}^{T} & \mathbf{0}^{T} & \mathbf{P}_{i}^{T} & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \mathbf{r}_{1} \\ \mathbf{r}_{2} \\ \mathbf{r}_{3} \\ \mathbf{T} \end{bmatrix} = \mathbf{P}_{i}^{\prime} ,$$

- each point pair yielding 3 equations, whereby at least four
- 4 point pairs are necessary to linearly solve for said rotation and
- 5 translation.
- 1 15. (Original) The linear method of claim 14, further
- 2 comprising the step of: decomposing said rotation matrix R using
- 3 Singular Value Decomposition (SVD) to obtain a form  $R = USV^T$ .

- 1 16. (Original) The linear method of claim 15, further
- 2 comprising the step of computing a new rotation matrix according to
- $_{3}$   $R = UV^{T}$
- 1 17. (Currently Amended) A program storage device readable by
- 2 machine, tangible embodying a program of instructions executable by
- 3 the machine to perform method steps for performing head motion
- 4 estimation from facial feature data, the method comprising the
- 5 steps of:
- 6 obtaining a first facial image and detecting a head in said
- 7 first image;
- detecting position of not more than only four points P of said
- 9 first facial image where  $P = \{p_1, p_2, p_3, p_4\}$ , and  $p_k = (x_k, y_k)$ ;
- obtaining a second facial image and detecting a head in said
- 11 second image;
- detecting position of not more than only four points P' of
- said first second facial image where  $P' = \{p'_1, p'_2, p'_3, p'_4\}$  and  $p'_k = (x'_k, y'_k)$ ;
- 14 and,
- determining the motion of the head represented by a rotation
- 16 matrix R and translation vector T using said points P and P'.

- 18. (Currently amended) The program storage device readable
  2 by machine as claimed in claim 17, wherein said only four points P
  3 of said first facial image and only four points P' of said second
  4 facial image include locations of outer corners of each eye and
  5 mouth of each respective first and second facial image.
- 1 19. (Original) The program storage device readable by
  2 machine as claimed in claim 17, wherein said head motion estimation
  3 is governed according to:

$$R = \begin{bmatrix} \mathbf{r}_{1}^{7} \\ \mathbf{r}_{2}^{T} \\ \mathbf{r}_{3}^{T} \end{bmatrix} = \begin{bmatrix} \mathbf{r}_{ij} \end{bmatrix}_{3\times 3}$$

$$\mathbf{T} = \begin{bmatrix} \mathbf{r}_{1} & T_{2} & T_{3} \end{bmatrix}^{T} \text{ represent}$$
and

- 5 camera rotation and translation respectively, said head pose
- 6 estimation being a specific instance of head motion estimation.
- 1 20. (Previously presented) A program storage device
- 2 readable by machine, tangible embodying a program of instructions
- 3 executable by the machine to perform method steps for performing
- 4 head motion estimation from facial feature data, the method
- 5 comprising the steps of:
- 6 obtaining a first facial image and detecting a head in said
- 7 first image;

- detecting position of four points P of said first facial image
- 9 where  $P = \{P_1, P_2, P_3, P_4\}$ , and  $P_k = (x_k, y_k)$ ;
- obtaining a second facial image and detecting a head in said
- 11 second image;
- detecting position of four points P' of said <u>first\_second</u>
- 13 facial image where  $P' = \{p'_1, p'_2, p'_3, p'_4\}$  and  $p'_k = (x'_k, y'_k)$ ; and
- determining the motion of the head represented by a rotation
- 15 matrix R and translation vector T using said points P and P',
- wherein said head motion estimation is governed according to:

$$R = \begin{bmatrix} \mathbf{r}_{i}^{T} \\ \mathbf{r}_{2}^{T} \\ \mathbf{r}_{3}^{T} \end{bmatrix} = \begin{bmatrix} \mathbf{r}_{ij} \end{bmatrix}_{3x3}$$

$$\mathbf{P}_{i}' = R\mathbf{P}_{i} + \mathbf{T}, \quad \text{where} \quad \mathbf{T} = \begin{bmatrix} \mathbf{r}_{ij} \\ \mathbf{r}_{3}^{T} \end{bmatrix} \quad \text{represent}$$

- 18 camera rotation and translation respectively, said head pose
- 19 estimation being a specific instance of head motion estimation, and
- wherein said head pose estimation is governed according to
- 21 said rotation matrix R, said method further comprising the steps
- 22 of:
- 23 determining rotation matrix R that maps points  $P_k$  to  $F_k$  for
- 24 characterizing a head pose, said points  $F_1, F_2, F_3, F_4$  representing three-
- 25 dimensional (3-D) coordinates of the respective four points of a
- reference, frontal view of said facial image, and  $\mathbf{P}_k$  is the three-

- 27 dimensional (3-D) coordinates of an arbitrary point where
- 28  $\mathbf{P}_i = [X_i \ Y_i \ Z_i]^T$ , said mapping governed according to the relation:

$$R(\mathbf{P}_2 - \mathbf{P}_1) \propto \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}^T$$

$$R(\mathbf{P}_6 - \mathbf{P}_5) \propto \begin{bmatrix} 0 & 1 & 0 \end{bmatrix}^T$$

31

- wherein  $P_5$  and  $P_6$  are midpoints of respective line segments
- connecting points  $P_1P_2$  and  $P_3P_4$  and, line segment connecting points
- $P_1P_2$  is orthogonal to a line segment connecting points  $P_5P_6$ , and
- $\infty$  indicates a proportionality factor.
- 1 21. (Previously presented) The program storage device
- 2 readable by machine as claimed in claim 20, wherein components rl,
- 3 r2 and r3 are computed as:

$$\mathbf{r}_2^T(\mathbf{P}_2 - \mathbf{P}_1) = 0$$
$$\mathbf{r}_3^T(\mathbf{P}_2 - \mathbf{P}_1) = 0$$

$$\mathbf{r}_1^T(\mathbf{P}_6-\mathbf{P}_5)=0$$

$$\mathbf{r}_3^T(\mathbf{P}_6-\mathbf{P}_5)=0$$

- 1 22. (Previously presented) The program storage device
- 2 readable by machine as claimed in claim 20, wherein components r1,
- 3 r2 and r3 are computed as:

US010476-aaf-09-16-05.doc

$$r_5 = (P_6 - P_5) \times (P_2 - P_1),$$

$$r_2 = r_3 \times (P_2 - P_1)$$

1 23. (Previously presented) The program storage device 2 readable by machine as claimed in claim 20, wherein

$$\begin{bmatrix} \mathbf{P}_i^T & \mathbf{0}^T & \mathbf{0}^T & \mathbf{1} & 0 & 0 \\ \mathbf{0}^T & \mathbf{P}_i^T & \mathbf{0}^T & 0 & 1 & 0 \\ \mathbf{0}^T & \mathbf{0}^T & \mathbf{P}_i^T & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \mathbf{r}_1 \\ \mathbf{r}_2 \\ \mathbf{r}_3 \\ \mathbf{T} \end{bmatrix} = \mathbf{P}_i'$$

- each point pair yielding 3 equations, whereby at least four point pairs are necessary to linearly solve for said rotation and translation.
  - 24. (Previously presented) The program storage device readable by machine as claimed in claim 23, further comprising the steps of decomposing said rotation matrix R using Singular Value Decomposition (SVD) to obtain a form  $R = USV^T$ .
    - 25. (Previously presented) The program storage device readable by machine as claimed in claim 23, further comprising the steps of computing a new rotation matrix according to  $R = UV^T$ .